

# Supporting Information for Photoabsorption Spectra of Small Na Clusters: TDHF and BSE versus CI and experiment

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This document contains time-dependent Hartree-Fock (TDHF), Bethe-Salpeter equation (BSE) and full CI (FCI) or quadruples CI (QCI, Ref. [1]) and multi-reference doubles CI (MRD-CI, Ref. [2]) excitation energies and oscillator strengths for  $D_{3h}$   $Na_5^+$ ,  $D_{3h}$  and  $D_{4h}$   $Na_6$  and  $D_{4d}$   $Na_8$  clusters. It also contains a density of HF energy levels for a  $C_3$   $Na_{20}$  cluster.

TABLE I.  $Na_5^+$   $D_{3h}$  excitation energies in eV and oscillator strengths, f.

State	TDHF	f	BSE	f	FCI <sup>a</sup>	f <sup>a</sup>
$1^1E'(x,y)$	2.58	0.47	2.58	0.05	-	-
$2^1E'(x,y)$	3.15	1.89	2.97	2.11	3.16	2.14
$1^1A_2''z$	2.02	0.67	2.15	0.91	2.23	0.96
$2^1A_2''z$	2.39	0.53	2.54	0.24	-	-

<sup>a</sup> Ref.[1]

TABLE II.  $Na_6$   $D_{3h}$  excitation energies in eV and oscillator strengths, f.

State	TDHF	f	BSE	f	QCI <sup>a</sup>	f <sup>a</sup>
$1^1E'(x,y)$	1.62	0.81	1.68	0.71	1.36	0.14 <sup>a</sup>
$1^1E'(x,y)$	2.07	2.28	2.12	2.20	1.94	2.64 <sup>a</sup>
$1^1E'(x,y)$	2.62	0.31	2.80	0.27	2.49	0.15
$1^1A_2''z$	2.62	0.93	2.80	0.99	2.81	0.81
$1^1A_2''z$	3.33	0.29	3.28	0.25	-	-
$1^1A_2''z$	3.43	0.14	-	-	-	-
$1^1A_2''z$	3.49	0.31	3.51	0.33	-	-
$1^1A_2''z$	4.99	0.19	4.87	0.27	-	-

<sup>a</sup> Ref.[1]

<sup>b</sup> Values corrected from those published in Ref. [1]. D. Rai (private communication).

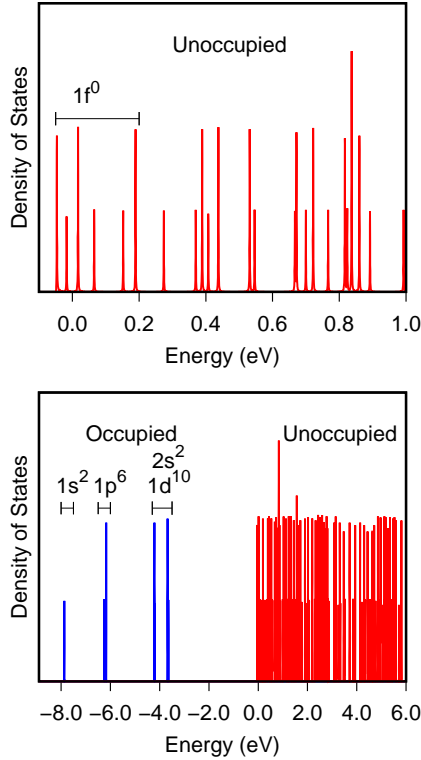


FIG. 1. Energy levels of  $Na_{20} C_3$  cluster indicated by vertical sticks. Upper panel shows virtual states up to 1 eV above the vacuum level and lower panel shows the shell structure in occupied and low energy virtual states.

TABLE III.  $Na_6$   $D_{4h}$  excitation energies in eV and oscillator strengths, f.

State	TDHF	f	BSE	f	QCI <sup>a</sup>	f <sup>a</sup>
$1^1E_u(x,y)$	1.54	0.45	1.77	0.44	1.65	0.28
$1^1E_u(x,y)$	1.96	0.27	2.17	0.66	1.90	0.04
$1^1E_u(x,y)$	2.23	2.22	2.40	1.89	2.34	1.30
$1^1E_u(x,y)$	3.06	0.32	3.16	0.29	-	-
$1^1A_{2u}z$	2.39	0.70	2.71	1.12	2.71	0.80
$1^1A_{2u}z$	3.26	0.84	3.29	0.45	-	-
$1^1A_{2u}z$	3.40	0.13	-	-	-	-
$1^1A_{2u}z$	4.76	0.17	4.72	0.26	-	-

<sup>a</sup> Ref.[1]

TABLE IV. Na<sub>8</sub> D<sub>4d</sub> excitation energies in eV and oscillator strengths, f.

State	TDHF <sup>a</sup>	f	BSE <sup>a</sup>	f	MRD-CI <sup>b</sup>	f
<sup>1</sup> E <sub>1</sub> (x, y)	1.29	0.03	1.33	0.01	1.45	0.46
<sup>1</sup> E <sub>1</sub> (x, y)	1.76	0.00	1.81	0.09	1.86	0.02
<sup>1</sup> E <sub>1</sub> (x, y)	1.90	0.47	2.04	0.30	1.97	0.29
<sup>1</sup> E <sub>1</sub> (x, y)	2.42	3.43	2.36	3.28	2.70	4.36
<sup>1</sup> E <sub>1</sub> (x, y)	2.94	0.18	3.14	0.12	-	-
<sup>1</sup> E <sub>1</sub> (x, y)	3.15	0.32	3.17	0.18	-	-
<sup>1</sup> E <sub>1</sub> (x, y)	3.32	0.14	3.50	0.29	-	-
<sup>1</sup> E <sub>1</sub> (x, y)	3.33	0.11	3.55	0.27	-	-
<sup>1</sup> B <sub>2</sub>	z 1.47	0.01	1.60	0.01	-	-
<sup>1</sup> B <sub>2</sub>	z 1.54	0.13	1.73	0.10	-	-
<sup>1</sup> B <sub>2</sub>	z 2.39	1.62	2.39	1.62	-	-
<sup>1</sup> B <sub>2</sub>	z 2.82	0.19	2.86	0.11	-	-
<sup>1</sup> B <sub>2</sub>	z 2.97	0.12	3.01	0.08	-	-
<sup>1</sup> B <sub>2</sub>	z 3.07	0.09	3.13	0.13	-	-
<sup>1</sup> B <sub>2</sub>	z 3.33	0.21	3.51	0.27	-	-
<sup>1</sup> B <sub>2</sub>	z 4.46	0.14	4.45	0.14	-	-

<sup>a</sup> This work

<sup>b</sup> Ref.[2]

<sup>1</sup> P. K. Priya, D. K. Rai, and A. Shukla, Eur. Phys. J. D **71**, 116 (2017).

<sup>2</sup> V. Bonačić-Koutecký, P. Fantucci, and J. Koutecký, Chem. Phys. Lett. **166**, 32 (1990).