Parametric relaxation in whispering gallery mode exciton-polariton condensates

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Polariton condensation of one-dimensional multimode whispering gallery mode exciton polaritons is investigated in hexagonal ZnO microwires at cryogenic temperatures. At threshold, stimulated scattering is fed by the resonant emission from highly populated defect-bound excitons. With further increasing excitation power, condensates relax within the multimode whispering gallery mode polaron ladder, leading to their effective evaporative cooling. The relaxation is a parametric polaron-polaron scattering process evidenced by its intensity, energy, and momentum evolution. The experimental observations are in good agreement with numerical simulations based on a model for polaron-polaron scattering extended to the multimodal whispering gallery mode system.

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Here, we demonstrate the condensation of WGM exciton polaritons at cryogenic temperature being accompanied by complex parametric polaron scattering processes. We observe an efficient exciton relaxation into defect-bound states, whose radiative decay resonantly excites the polaron condensate above threshold in one of the many lower polaron branches. By increasing the excitation power, condensate relaxation into further lower polaron states takes place, providing an efficient evaporative cooling mechanism. We show experimentally and theoretically that this process is caused by multichannel scattering mechanisms leading to parametric mixing of polaron states at higher excitation densities, as evidenced by constant energy and momentum steps between the different polaron states. We believe that these multimode parametric mixing processes pave the way towards polaron entanglement.

Figure 1 shows typical angle-resolved photoluminescence (PL) images (cw excitation) of a ZnO microwire recorded at 10 K. Besides prominent transitions of free excitons (X), donor-bound excitons (D0,X) [14], and defect-bound excitons (DBX) [15], it clearly shows dispersion behavior of confined modes evidenced by the increase of the mode energy with the emission angle, or equivalently the wave vector. Note that the PL image is recorded unpolarized and shows contributions from transverse electric (TE)- and transverse magnetic (TM)-polarized modes. In order to assess if WGMs and ZnO excitons strongly interact with each other, a careful remodeling of the photonic WGM dispersion curves is indispensable. In our case, we determine an average coupling strength of around 100 meV between ZnO excitons and WGM photons (see Ref. [16] for details), which is in very good agreement with earlier publications [17]. Figure 1 shows that the WGM exciton-polariton system is multimodal, i.e., several photonic WGMs with different axial mode numbers strongly couple to the excitonic transitions [18]. In the present case, the WGM ground state (N_{WGM} = 1) has an energy far below the exciton resonance (which is close to N_{WGM} ≈ 200), thus it does not play any role in the strong interaction between cavity photons and excitons.

Excitation-dependent PL images (pulsed excitation) recorded at T = 10 K from a ZnO microwire are shown...
in Fig. 2 (top). Below threshold, transitions of donor-bound excitons dominate the PL and a weak emission is visible around 3.337 eV, which can be related to defect-bound excitons (DBX). When increasing the excitation intensity to $P_0 = 1.5$ kW/cm², the system reaches the lasing regime (evidenced by the buildup of spatial coherence—see Ref. [16]). At threshold, emission around the DBX transition becomes more pronounced and even dominating at further high excitation power. Simultaneously, more peaks appear at energies above and below this initial state as well as at the spectral positions of the polariton states. A closer look at these peaks (see the white-framed inset in Fig. 2, top) reveals that the emission clearly arises from two spots symmetrically shifted from $k = 0$ with the following two properties: The emission does not originate from the dispersion minimum but is blueshifted by $\Delta E_B = 0.3$ meV and arises at a finite and discrete wave vector $k_\parallel \approx \pm 0.01 \mu$m⁻¹. Both properties are strong indications for polariton condensation and can be clearly distinguished from the photon lasing regime (see Ref. [16] for details). The finite $k_\parallel$ indicates finite momentum of the involved quasiparticles, gained either by scattering processes or by acceleration along the wire axis away from an inhomogeneous potential landscape [11,19]. The latter can be ruled out since our excitation spot size is much larger than the field of view of our microscope setup (please see Ref. [16] for setup details). We therefore do not expect an inhomogeneous background potential induced by the photogenerated exciton reservoir to be present in the collection area.

It can be seen in Fig. 2 that almost no WGM polariton states are occupied at energies above the initial condensate state (around 3.337 eV). Apart from that, this energy only coincides with any free-exciton- or phonon-assisted process, which is why we exclude any relaxation process involving exciton-donor bound exciton, exciton-phonon, polariton-phonon, or interbranch polariton-polariton scattering from the highest lower polariton branch (respectively the free exciton reservoir) into this state. Instead, we propose that the initial condensate state is resonantly excited by the radiative decay of DBX, which are highly occupied at low temperatures due to efficient and fast energy relaxation of free excitons [20,21]. This is a very efficient process since DBX within the whole excitation volume contribute to the excitation of the surface near WGM polariton states.

By further increasing the excitation power, polariton states at lower energies also turn into the condensation regime, i.e., the polariton condensate relaxes into energetically lower polariton states (as can also be seen in momentum space [16]). A remarkable feature of the relaxation process is the increase in the condensate wave vector. That this relaxation can take place at all is a consequence of the multimodality of the WGM exciton-polariton system [13]. In contrast to common semiconductor microcavities where polaritons relax into the system’s ground state and experience a strong interparticle interaction, polaritons in multimode systems efficiently relax into lower states when occupation of one of the initial state is reached [22]. Thus, the occupation of each of the initial states is almost clamped to their particular threshold values. As a consequence, the polariton-polariton interaction-driven blueshift of the condensate energy in each of the discrete condensate states is much smaller compared to single mode systems and is almost independent of the excitation power. In the experiment, $\Delta E_B$ is found to be nearly constant above threshold, which reflects this behavior, but also means that the total charge carrier density does not increase further and a quasisteady state is reached. In principle, the energetically lowest target state which can be reached by such a relaxation process should be set by the coupling strength between the exciton and WGM photon as well as their lifetimes.

We simplify the complex process by a scheme depicted in Fig. 2 (bottom) showing a magnified view of the condensation region. Due to an increase of occupation of the initially fed states (around the DBX energy), polaritons scattering into the surrounding states sets in. However, condensation is reached first in the initial state at $k_\parallel \approx 0$. With further increasing density, the repulsive interaction between polaritons becomes efficient and polariton-polariton scattering into several branches is observed. Hereby, two polaritons scatter out of the initial state into states with higher as well as lower energy and higher momentum. Since polaritons with higher energy are more excitonlike than lower-energy polaritons and therefore possess a shorter lifetime (in the presented microwire the excitonic lifetime at 4 K is \( \approx 500 \) fs compared to a 1–2 ps photonic lifetime), high-energy particles are effectively removed from the system. This process can be understood as an evaporative cooling of the condensate. Besides that, fast relaxation from high-energy states into the initial states or low-energy states can take place. This is supported by the strong suppression of emission above the DBX energy.

The process of relaxation is further analyzed in a magnified section of the PL image with highest excitation of Fig. 2 (top) and shown in Fig. 3(a) together with the calculated TE-polarized polariton dispersion curves (white dotted lines). It is obvious that only TE-polarized polaritons undergo condensation and relaxation whereas TM-polarized modes
FIG. 2. (Color online) Top: Excitation-dependent, normalized PL images ($T = 10$ K) of a ZnO microwire ($P_0 = 15$ kW/cm$^2$). Relative excitation powers as well as intensity multiplication factors are given at the bottom of each image. The white frame shows a magnified image of the condensation region at threshold. Middle: Simulated polariton relaxation for increasing pump powers $F_p = \{0.1, 0.2, 0.3, 0.4, 0.5\}$ in arbitrary units (left to right). The WGM polariton dispersions are shown by the dashed lines. Bottom: Schematic of the excitation power-dependent scattering processes. Note that only one out of many scattering paths is shown for clarity. Occupied polariton states are shown as circles and the color code from light orange to red indicates increasing occupation density. The blue circles indicate target states not visible in the PL images due to their fast decay and relaxation. Red arrows refer to linear polariton-polariton scattering while black arrows indicate parametric mixing processes.

FIG. 3. (Color online) (a) PL image and (b) simulation from Fig. 2 for highest excitation ($P = 2.8 P_0$) in a magnified view. The dotted white lines represent the calculated, TE-polarized WGM exciton-polariton dispersion curves. Above: Momentum profile of image below. The profile is shown for the spectral position marked by the gray and purple arrow. Note that the asymmetry in the emission pattern for positive and negative emission angles might be caused by the slight posture of the wire. (c) Extracted energies and momenta of the experimental polariton condensate states. The linear, dotted black lines are guide to the eyes. The gray dotted lines are calculated dispersion curves. The respective polariton mode numbers are given on the left side. Possible parametric scattering events are sketched by blue arrows in (a)–(c).
show some emission at the bottom of the dispersion near zero wave vector. This is reasonable since two-dimensional photons (propagating in the cross section plane) only couple to three-dimensional excitons with a suitable wave vector and polarization. Since highly occupied A-exciton states in ZnO are mainly TE polarized [23], they predominantly couple to TE-polarized photons to form polaritons. Our observation is also consistent with Ref. [24], where only TE-polarized WGMs switch to the photonic lasing regime.

Having a closer look at a momentum profile [see Fig. 3(a), top] integrated over a narrow energy range around one of the condensate levels (at ≈3.3262 eV), we see that at least two pronounced relaxation paths exist (highlighted by squares). For analysis, we extracted the energy and momentum values of all these condensate states and plotted them in Fig. 3(c). It can be seen that both relaxation paths are linear below a certain energy, revealing constant energy and momentum steps between the individual polariton states. The observed constant energy and momentum steps between adjacent states indicate parametric polariton-polariton scattering to be dominant above threshold. This process sets in when the population of distinct initial and target states is high enough. The energy-momentum conservation condition thereby is fulfilled at least for two relaxation paths, with similar merging points of the condensate ladders slightly below the initial state. The complex scattering behavior is also reflected in the observed complex, noncontinuous intensity evolution of the individual states (not shown). Some possible scattering events of the two processes are sketched in Fig. 2 (bottom).

In order to theoretically substantiate our experimental observations, we deduced a model that is able to describe polariton-polariton scattering events in a multimodal polariton system. The model is based on equations derived in Refs. [25,26] and is extended to the whispering gallery mode system with its multimodal structure. The Hamiltonian in the polariton basis reads

\[ H = H_{LP} + H_{PP} + H_F. \] (1)

The first term \( H_{LP} \) is the free evolution of the polaritons,

\[ H_{LP} = \sum_{i=1}^{N} \sum_{k} E_{\text{LP}}^{(i)}(k) \hat{p}_{k,i}^{+} \hat{p}_{k,i}, \] (2)

where \( N \) is the number of lower polariton branches in the WGM resonator and \( \hat{p}_{k,i}^{+} (\hat{p}_{k,i}) \) is the polariton creation (annihilation) operator for the polaritons with wave vector \( k \) in the polariton branch \( i \). The polariton-polariton interaction is described by

\[ H_{PP} = \sum_{h,i,j,k,k',q} V_{h,i,j,k,k',q} \hat{p}_{k,i}^{+} \hat{p}_{k',j} \hat{p}_{k,q}^{+} \hat{p}_{k-h,j} \] (3)

The interaction potential \( V \) comes from the exciton-exciton interaction and can be written as

\[ V_{h,i,j,k,k',q} = \frac{\lambda_X}{A} \frac{6e^2}{\epsilon} X_{k,q-j} X_{k'-j} X_{k-h} X_{k',h}, \] (4)

where \( X \) is the excitonic fraction of the corresponding polariton state and \( \lambda_X \) is the exciton Bohr radius (2.87 nm). The excitation area is denoted by \( A \). Note that we neglect the saturation of the exciton and consider solely a linear coupling, in contrast to Refs. [25,26]. Finally, we consider the polariton–driving field interaction, which is given by

\[ H_F = \sum_{k,i} \Omega_{pr}(t) \hat{c}_{k,i} \hat{p}_{k,i}^{+} + \Omega_{pr}(t) C_{k,i} \hat{p}_{k,i}^{+} + H.c. \] (5)

The first term corresponds to a weak probe field \( \Omega_{pr} \) incident on all polariton states, which represents a small thermal population. This is required to initiate the parametric scattering process. The second term is a strong pump field \( \Omega_{p} \) acting only on a single polariton state with \( k_0 \) and in the branch \( i_0 \), which represents the resonant feeding of the polariton mode by the defect-bound exciton. The terms are weighted by the cavity fraction \( C \) of the corresponding state.

The optical response of the probe beam is given by the expectation value \( P_{k-q,i} = \langle p_{k-q,i} \rangle \) which couples through polariton-polariton interactions to the state \( P_{k,h} = \langle p_{k,h} \rangle \). The polariton-polariton diffusion produces a wave-mixing component in one of the polariton branches at wave vector \( k + q \). Of course this only holds if the energy \( E_{\text{LP}}^{(i)}(k + q) + E_{\text{LP}}^{(j)}(k - q) - 2 E_{\text{LP}}(k) = 0 \) is conserved. Note that \( |P_{k,i}|^2 \) represents the polariton occupation with wave vector \( k \) in mode \( i \). While in the typical case with a single lower polariton branch only one configuration of \( k \) and \( q \) fulfills the above requirement of energy and momentum conservation, a multimodal structure leads to a variety of possible scattering channels. In addition to momentum and energy conservation, parity conservation also needs to be taken into account in multimodal systems [5].

The system reaches even more complexity as each of the polariton modes, populated by parametric scattering, can be a superposition of many individual polariton states. Numerical simulations of the energy-momentum space distribution of the polariton occupation are shown in Fig. 2 (middle) for different excitation powers. We have chosen parameter values typical for ZnO or which we have derived from the experiment (as discussed above). The numerical results reproduce the experimental observations very well and thus confirm the model of parametric mixing of polariton
states. Especially, the occupation of more and more low-energy states with increasing excitation power and the two main relaxation paths with its discrete energy-momentum states are reproduced. An obvious difference between the experimental observations and the modeling is the high occupation of polariton modes with energies above the excitation energy. This is caused by the limited number of dispersions taken into account in the simulations in order to maintain reasonable computation times. Furthermore, the polariton dispersions used are fitted using a coupled oscillator model, which enables one to assign angle- and mode-dependent photonic and excitonic fractions to the dispersions. We assume that all WGM modes have the same quality factor $Q = 8000$ and an exciton-photon coupling of 80 meV. This very simplified approach results in high excitonic fractions of polariton states with high energies and thus increases the parametric scattering into these states. However, both reasons for the accumulation of polaritons in these high-energy modes do not affect the relaxation into the lower polariton states since no direct scattering channels are allowed.

In conclusion, polariton condensation accompanied by parametric polariton mixing has been experimentally observed and theoretically simulated in a one-dimensional multimode whispering gallery mode polariton system. The initial mode is resonantly excited by the radiative decay of defect-bound excitons, energetically far away from the free and donor-bound exciton transitions. With increasing excitation power, the parametric mixing process causes cooling of the polariton system by an effective energetic net relaxation, accompanied by momentum gain for low-energy states. The observed scattering properties resemble well the requirements for the creation of branch entangled polaritons. Especially, the intersubbranch scattering solely in the lower polariton branches and the internal resonant excitation of the initial mode at $k_0 = 0$ provides a polariton system that is well isolated from the excitonic reservoir, as discussed in Ref. [8]. Thus we propose that one-dimensional ZnO microwires provide an excellent system for polariton lasing and entanglement as a source of entangled photons for future integrated quantum computing and communication applications.

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