



## **JF Physical Chemistry 2010-2011.**

### **JF CH 1101: Introduction to Physical Chemistry.**

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**A compendium of past examination questions set on Physical Chemistry on the JF Chemistry paper and problem sheets associated with CH1101 Physical Chemistry (Lyons).**

This booklet has been produced to provide JF Chemistry students with a full selection of problems in basic Physical Chemistry set by the author over the last few years. These problems have appeared in the Annual, and the Supplemental examination papers in Chemistry set by the Examination Board of the School of Chemistry, University of Dublin, Trinity College.

They are made available to Trinity JF Chemistry students to assist them in their revision of the basic Physical Chemistry lectures on properties of Gases, Thermodynamics, Equilibria and Electrochemistry delivered by Dr Lyons in the first semester to students taking CH 1101.

I hope that you will find it a useful self learning and revision aid.

Mike Lyons  
1 September 2010

## JF Chemistry Module CH1101. 2009

### MCQ Semester 1 Test

1. Consider the synthesis of ammonia which proceeds according to the following reaction:  $\frac{1}{2} \text{N}_2(\text{g}) + \frac{3}{2} \text{H}_2(\text{g}) \rightarrow \text{NH}_3(\text{g})$ . If the standard change in Gibbs energy for the reaction is given by  $\Delta_r G^0 = -16,370 \text{ J mol}^{-1}$  at  $T = 298 \text{ K}$  then the equilibrium constant  $K$  for the reaction is:

- (a)  $7.38 \times 10^2$  **(Answer)**  
(b)  $7.38 \times 10^{-2}$   
(c) 0.1  
(d) 100  
(e) there is insufficient data supplied to answer the question.

You may assume that the gas constant  $R = 8.314 \text{ J mol}^{-1} \text{ K}^{-1}$ .

2. In air at 298 K which gas has the lowest average root mean square speed?

- (a)  $\text{H}_2\text{O}(\text{g})$ ; (b)  $\text{CO}_2(\text{g})$  **(Answer)**; (c)  $\text{CO}(\text{g})$ ; (d)  $\text{Ne}(\text{g})$ ; (e)  $\text{CH}_4(\text{g})$ .

3. For ideal gases which of the following statements are **correct**?

- i. At constant temperature, the volume of a fixed mass of gas is proportional to the external pressure.
- ii. At constant external pressure and temperature, when 1L of  $\text{N}_2$  reacts with 2L of  $\text{O}_2$ , 2L of  $\text{NO}_2$  are formed
- iii. At a given temperature and external pressure, equal volumes of any ideal gas contain the same number of molecules
- iv. At a given temperature, the molecules in any ideal gas have the same average velocity
- v. At a given pressure and temperature, the mean-free path of a gas is independent of the volume of the containing vessel

- a)** (ii) and (iii)  
**b)** (i), (iii) and (v)  
**c)** (ii) and (iii)

- d) (ii) and (v)  
e) (ii), (iii) and (v)    **(Answer)**

## Section A Long Questions 2009

### Annual

- (a) Briefly discuss the concept of pH as applied to aqueous solutions paying attention to its definition and measurement.
- (b) Draw the shape expected for the titration curve expected for a titration of a strong acid by a strong base and between a weak acid and a strong base. You should describe features of interest associated with each of these titration curves.

Consider the titration of 100 mL of 0.1 M acetic acid with 0.1 M NaOH. (i) What is the pH of the solution when 90 mL of 0.1 M NaOH has been added to 100 mL of 0.1 M acetic acid. (ii) Determine the pH at the equivalence point. (iii) What is the pH after 110 mL of 0.1 M NaOH has been added.

### Supplemental

- (a) Define the terms oxidation, reduction, galvanic cell, electrolysis cell.
- (b) Describe using a suitable example, with a labelled diagram and pertinent chemical equations, how a fuel cell operates.
- (c) Derive and state the relationship between the change in Gibbs free energy  $\Delta G$  and the open circuit cell potential  $E_{\text{cell}}$ .
- (d) Calculate the equilibrium constant at 298 K for the reaction  $Fe(s) + Cd^{2+}(aq) \rightleftharpoons Fe^{2+}(aq) + Cd(s)$  given that the standard reduction potentials are  $E^{\circ}(Cd^{2+}, Cd) = -0.40 \text{ V}$  and  $E^{\circ}(Fe^{2+}, Fe) = -0.44 \text{ V}$ . Is the reaction strongly product favoured?

## Section B MCQ 2009

### Annual

1. Consider the following reaction:  $\text{N}_2(\text{g}) + 3\text{H}_2(\text{g}) \rightleftharpoons 2\text{NH}_3(\text{g})$ . At equilibrium at a certain temperature the concentrations of  $\text{NH}_3(\text{g})$ ,  $\text{H}_2(\text{g})$  and  $\text{N}_2(\text{g})$  are 0.94 M, 1.60 M and 0.52 M respectively. The numerical value of the equilibrium constant  $K_c$  for the reaction is: (a) 0.415 ; (b) 1.13; (c) 1.06; (d) 0.664; (e) 1.27. Correct answer: a.
2. Calculate the concentration of  $\text{OH}^-$  ion for an aqueous solution with a pH of 9.45. Note that the ion product of water  $K_w = 1 \times 10^{-14}$ . (a)  $1.8 \times 10^{-10}$  M ; (b)  $1.0 \times 10^{-14}$  M ; (c)  $2.8 \times 10^{-5}$  M ; (d) 0.35 M ; (e)  $3.5 \times 10^{-10}$  M. Correct answer: c
3. A buffer contains equal concentrations of a weak acid HA and its conjugate base  $\text{A}^-$ . If the value of  $K_A$  for the weak acid is  $1.0 \times 10^{-9}$ , what is the pH of the buffer? (a) 9.0 ; (b) 5.0 ; (c) 1.0; (d) 13.0 ; (e) 7.0. Correct answer: a.
4. If the standard potential  $E^0$  is 0.56 V at 298 K for the cell reaction:  $\text{Cr}_2\text{O}_7^{2-}(\text{aq}) + 6\text{Fe}^{2+}(\text{aq}) + 14\text{H}^+(\text{aq}) \rightarrow 2\text{Cr}^{3+}(\text{aq}) + 6\text{Fe}^{3+}(\text{aq}) + 7\text{H}_2\text{O}(\text{l})$  calculate the equilibrium constant for the reaction. (a)  $6.2 \times 10^{56}$  ; (b) 37.8 ; (c)  $2.9 \times 10^9$  ; (d)  $2.5 \times 10^{28}$  ; (e)  $1.4 \times 10^3$ . Correct answer: a.

### Supplemental

1. Consider the reaction:  $\text{N}_2(\text{g}) + 3\text{H}_2(\text{g}) \rightleftharpoons 2\text{NH}_3(\text{g})$ . If the standard molar free energy of formation of  $\text{NH}_3(\text{g})$  at 298 K is  $-16.45 \text{ kJ mol}^{-1}$ , calculate the equilibrium constant for this reaction at 298 K. (a)  $3.62 \times 10^{-2}$  ; (b)  $1.66 \times 10^{-3}$  ; (c)  $5.26 \times 10^{-14}$  ; (d)  $1.71 \times 10^{-6}$  ; (e)  $2.29 \times 10^{-7}$ . Correct answer: d.
2. The pH of 0.1 M  $\text{CH}_3\text{COOH}$  is 2.87. What is the value of  $K_A$  for  $\text{CH}_3\text{COOH}$ ? (a)  $1.3 \times 10^{-3}$  ; (b)  $1.8 \times 10^{-6}$  ; (c)  $1.8 \times 10^{-5}$  ; (d) 0.037; (e)  $2.7 \times 10^{-6}$ . Correct answer: c.
3. The conjugate base of  $\text{HSO}_4^-$  is: (a)  $\text{OH}^-$  ; (b)  $\text{SO}_4^{2-}$  ; (c)  $\text{H}_2\text{SO}_4$ ; (d)  $\text{HSO}_4^-$  (e)  $\text{H}_2\text{O}$ . Correct answer: b.

4. The standard potential of the  $\text{Ag}^+|\text{Ag}$  redox couple is + 0.80 V and the standard potential of the cell  $\text{Fe(s)}|\text{Fe}^{2+}(\text{aq})||\text{Ag}^+(\text{aq})|\text{Ag(s)}$  is + 1.24 V. What is the standard potential of the  $\text{Fe}^{2+}|\text{Fe}$  redox couple?
- (a) 2.04 V ; (b) - 0.44 V; (c) - 2.04 V ; (d) + 0.44 V ; (e) - 0.88 V. Correct answer: b.

**JF Chemistry Module CH 1101 2010. Dr Mike Lyons**

**Section A Long Questions 2010.**

**Annual.**

1.

Answer **either** : part (a) and part (b) **or** part (c) and part (d).

- a. What is the internal energy  $U$  and the enthalpy  $H$  of a system? Write down an expression for the First Law of Thermodynamics which relates the change in internal energy of a system to the work done on the system and the heat absorbed by the system. Hence derive a relationship between the change in internal energy  $\Delta U$  and the change in enthalpy  $\Delta H$  of a system.
- b. A gas absorbs 300 J of heat and at the same time expands by 1 dm<sup>3</sup> against a constant pressure of 1 atm. What is the change in internal energy  $\Delta U$  and change in enthalpy  $\Delta H$  of the system.
- c. Define the term heat capacity and briefly describe using a labelled diagram and any equations where pertinent how the bomb calorimeter can be used to measure the change in internal energy of combustion of a material.
- d. Inside in a bomb calorimeter, 1.0 g of octane  $C_8H_{18}$  combusts in oxygen to form carbon dioxide and water according to the expression  $C_8H_{18} + 25/2O_2 \rightarrow 8CO_2 + 9H_2O$ . The temperature was observed to rise from 25.00 to 33.20 °C. The calorimeter contained 1200 g of water (specific heat capacity of water = 4.184 Jg<sup>-1</sup>K<sup>-1</sup>) and the heat capacity of the bomb is 837 JK<sup>-1</sup>. Calculate the internal energy of combustion of octane.

2. Answer all parts.

- (a) Briefly explain using specific examples and clearly labelled diagrams how a Galvanic (Voltaic) cell and how a Polymer Membrane Electrolyte (PEM) fuel cell operates.
- (b) The net reaction that occurs in a voltaic cell is  $Zn(s) + 2Ag^+(aq) \rightarrow Zn^{2+}(aq) + 2Ag(s)$ . Write down the half reactions that occur at the anode and cathode. If the standard

reduction potentials at 298K are  $E^0(\text{Ag}^+, \text{Ag}) = 0.799\text{V}$  and  $E^0(\text{Zn}^{2+}, \text{Zn}) = -0.763\text{V}$ , calculate the voltage developed by the cell, the change in reaction Gibbs energy  $\Delta G^0$  and the equilibrium constant  $K$  for the cell reaction. Is the reaction strongly product favoured?

- (c) Consider a galvanic cell involving the following half-reactions:  $\text{Ni}^{2+}(\text{aq}) + 2\text{e}^- \rightarrow \text{Ni}(\text{s})$ ,  $E^0(\text{Ni}^{2+}, \text{Ni}) = -0.25\text{V}$ ;  $\text{Cr}^{3+}(\text{aq}) + 3\text{e}^- \rightarrow \text{Cr}(\text{s})$ ,  $E^0(\text{Cr}^{3+}, \text{Cr}) = -0.74\text{V}$ . Calculate the cell potential observed at a temperature of 298 K when  $[\text{Ni}^{2+}] = 1.0 \times 10^{-4}\text{M}$  and  $[\text{Cr}^{3+}] = 2.0 \times 10^{-3}\text{M}$ .

### Supplemental 2010.

- (a) A strip of magnesium metal of mass 12.5 g is dropped into a beaker of dilute hydrochloric acid. Given that the Mg is the limiting reactant, calculate the work done by the system as a result of the reaction. The atmospheric pressure is 1 atm and the temperature is 293.2 K.

(b) If the enthalpy of combustion of solid citric acid is  $-1986\text{ kJ mol}^{-1}$ , calculate the heat liberated when 10 g of solid citric acid undergoes total combustion at 298 K: (i) at constant pressure, (ii) at constant volume. Note: citric acid has formula  $\text{C}_6\text{H}_8\text{O}_7$ . The molar mass  $M = 192\text{ g mol}^{-1}$ . Total combustion means reaction with  $\text{O}_2$  and conversion to  $\text{CO}_2$  and  $\text{H}_2\text{O}$ .
- Answer **four** parts.
  - What do you understand by the terms weak acid and solution pH? Provide an example of a weak acid and indicate the way that the acid strength of a weak acid can be quantified.
  - Calculate the pH of a  $5.0 \times 10^{-2}\text{ M}$  NaOH solution given the information that  $K_w = 1.0 \times 10^{-14}$ .
  - Calculate the  $\text{H}_3\text{O}^+$  ion concentration and the pH of a 0.003 M  $\text{Ba}(\text{OH})_2$  solution assuming that the ion product  $K_w = 1.0 \times 10^{-14}$ .
  - Derive an expression for the pH of an aqueous solution of weak acid HA of concentration  $c$  and having an acid dissociation

constant  $K_A$ . If  $K_A$  is assumed to be very small derive an approximate expression for the solution pH mentioning any approximations which you make.

- (e) Use the theoretical results derived in part (d) to calculate the pH of a weak acid solution of concentration 0.1 M and having an acid dissociation constant  $K_A = 3.5 \times 10^{-8}$ .

### Section B MCQ.

#### Annual.

1. Which of the following graphs does not give a straight line for an ideal gas? (a) V versus T, (b) T versus P, (c) P versus 1/V, (d) n versus 1/T, (e) n versus 1/P. (correct answer option (e)).
2. Which of the following statements is always true for an ideal gas?
  - (a) If the temperature and volume of a gas both increase at constant pressure, the amount of gas must also increase.
  - (b) If the pressure increases and the temperature decreases for a constant amount of gas, the volume must decrease.
  - (c) If the volume and the amount of gas both decrease at constant temperature, the pressure must decrease.

(Correct answer option (b)).

3. A solution has a hydrogen ion concentration of 0.001 M. Which of the following statements are correct? (i) The solution pH is 3.0. (ii) The solution is acidic. (iii) The hydroxide ion concentration is  $1.0 \times 10^{-11}$ . Note that  $K_w = 10^{-14}$ .
  - (a) All statements are correct.
  - (b) (i) only.
  - (c) (i) and (ii) only.
  - (d) (iii) only.
  - (e) None of the statements are correct.

(Correct answer option (a)).

4. Given that  $K_a$  (acetic acid) =  $1.80 \times 10^{-5}$  and  $K_w = 1.0 \times 10^{-14}$  then the pH of an 0.89 M solution of sodium acetate is : (a) 9.35, (b) 7.0, (c) 5.0, (d) 13.0 and (e) 3.0. (Option (a) is correct).



5. The Galvanic cell  $Cu|Cu^{2+}(aq)||Ag^+(aq)|Ag$  is based on the following cell reaction:  $2Ag^+(aq) + Cu(s) \rightarrow 2Ag(s) + Cu^{2+}(aq)$ . Note that  $T = 298$  K and the standard electrode potentials are  $E^0(Cu^{2+}, Cu) = 0.34V$  and  $E^0(Ag^+, Ag) = 0.80V$ . Which of the following statements are correct?
- (i) The silver electrode is the cathode and the copper electrode is the anode. (ii) Two moles of electrons flow through the external circuit from anode to cathode when the cell operates. (iii) The observed cell potential is 0.46 V. (iv) The change in Gibbs energy for the cell reaction is  $-88,766 \text{ J mol}^{-1}$ .
- (a) All statements are correct.  
 (b) (i) only.  
 (c) (i) and (ii) only.  
 (d) (iii) and (iv) only.  
 (e) None of the statements are correct.

(Option (a) is correct).

6. Which of the following statements pertaining to ideal gases are correct? (i) The average kinetic energy of a gas molecule is proportional to the absolute temperature  $T$  of the gas sample. (ii) The ratio of the velocities by which two different types of ideal gas molecules A and B move is given by  $\frac{v_A}{v_B} = \sqrt{\frac{m_B}{m_A}}$  where  $m$  and  $v$  denote the mass and velocity of the molecules. (iii) The average velocity of a  $H_2$  molecule at 273 K is  $2000 \text{ ms}^{-1}$  if the average velocity of an  $O_2$  molecule at this temperature is  $500 \text{ ms}^{-1}$ . (iv) The heavier the gas molecule is the quicker it travels through the container.
- (a) All statements are correct.  
 (b) (i), (ii) and (iii) are correct.  
 (c) (iv) is correct.  
 (d) (iii) is correct.  
 (e) None of the statements are correct.

(Option (b) is correct).

7. Which of the following is the correct expression for the equilibrium constant for the reaction:  $2NO_2(g) \rightleftharpoons 2NO(g) + O_2(g)$

(a)  $K_c = \frac{[NO_2]}{[NO][O_2]}$ , (b)  $K_c = \frac{[NO][O_2]}{[NO_2]}$ , (c)  $K_c = \frac{[NO_2]^2}{[NO]^2[O_2]}$ ,

(d)  $K_c = \frac{[NO]^2[O_2]}{[NO_2]^2}$ , (e)  $K_c = \frac{[2NO]^2[O_2]}{[2NO_2]^2}$

(Option (d) is correct).

### Supplemental.

1. Which of the following graphs does not give a straight line for an ideal gas? (a) P versus V, (b) P versus T, (c) V versus T, (d) Average kinetic energy vs T, (e) P versus n. (correct answer option (a)).

2. The equilibrium constant for the reaction of hydrogen gas and ethene to produce ethane under certain conditions is  $9.8 \times 10^{18}$ .  $H_2(g) + C_2H_4(g) \rightleftharpoons C_2H_6(g)$   $K = 9.8 \times 10^{18}$ . What is the equilibrium constant for the following reaction  $C_2H_6(g) \rightleftharpoons H_2(g) + C_2H_4(g)$  under the same conditions? (a)  $-9.8 \times 10^{18}$ . (b)  $-4.9 \times 10^{18}$ . (c)  $1.9 \times 10^{19}$ . (d)  $9.8 \times 10^{-18}$ . (e)  $1.0 \times 10^{-19}$ .

(Correct answer : option (e)).

3. The thermodynamic equilibrium constant for the following reaction  $2 SO_2(g) + O_2(g) \rightleftharpoons 2 SO_3(g)$  is 0.15 at  $1227^\circ C$ . Which of the following statements are true? (i) The reaction is strongly product favoured. (ii) The reaction is reactant favoured. (iii) The change in Gibbs energy is negative. (iv) The change in Gibbs energy is  $23.66 \text{ kJ mol}^{-1}$ .

- (a) All statements are correct.  
 (b) (i) is correct.  
 (c) (ii) and (iv) are correct.  
 (d) (iii) is correct.  
 (e) None of the statements are correct.

(Correct option : answer (c)).

4. Which of the following statements pertaining to acids and bases are correct? (i) Acids are species which accept protons. (ii) Acid solutions have a pH value greater than 7. (iii) bases are species which donate protons. (iv) The pH of a base solution is less than 7. (v) The weaker the Bronsted Lowry acid the stronger is the conjugate base.

- (a) All statements are correct.
- (b) None of the statements are correct.
- (c) (i) and (ii) are correct.
- (d) (v) is correct.
- (e) (iii) and (iv) are correct.

(Correct answer: option (d)).

5. The Galvanic cell  $Zn|Zn^{2+}(aq)||Cu^{2+}(aq)|Cu$  is based on the following cell reaction:  $2Cu^{2+}(aq) + Zn(s) \rightarrow 2Cu(s) + Zn^{2+}(aq)$ . Note that  $T = 298\text{ K}$  and the standard electrode potentials are  $E^0(Cu^{2+}, Cu) = 0.34V$  and  $E^0(Zn^{2+}, Zn) = -0.76V$ . Which of the following statements are correct? (i) The copper electrode is the cathode and the zinc electrode is the anode. (ii) Two moles of electrons flow through the external circuit from anode to cathode when the cell operates. (iii) The observed cell potential is 1.10 V. (iv) The change in Gibbs energy for the cell reaction is  $-212,300\text{ J mol}^{-1}$ .

- (a) All statements are correct.
- (b) (i) only.
- (c) (i) and (ii) only.
- (d) (iii) and (iv) only.
- (e) None of the statements are correct.

(Option (a) is correct).

6. Which of the following is the correct expression for the equilibrium constant for the reaction:  $2A(g) \rightleftharpoons 2B(g) + C(g)$

(a)  $K_c = \frac{[A]}{[B][C]}$ , (b)  $K_c = \frac{[B][C]}{[A]}$ , (c)  $K_c = \frac{[A]^2}{[B]^2[C]}$ ,

(d)  $K_c = \frac{[B]^2[C]}{[A]^2}$ , (e)  $K_c = \frac{[2B]^2[O_2]}{[2A]^2}$ . (Correct option = (d)).

7. On the space shuttle, the carbon dioxide produced by the astronauts is handled by an environmental control system that utilizes the following reaction.



If the standard change in enthalpy and entropy for the reaction are  $\Delta H^\circ = -138.4 \text{ kJ}$  and  $\Delta S^\circ = -139 \text{ J/K}$ , then the standard change in Gibbs energy  $\Delta G^\circ$  at 298 K for this reaction is : (a)  $4.13 \times 10^4 \text{ kJ}$ . (b)  $-135 \text{ kJ}$ . (c)  $-180 \text{ kJ}$ . (d)  $-97.0 \text{ kJ}$ . (Correct answer option (d)).

## JF Chemistry Module CH1101.

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### Problem Sheet 1.

#### Introduction to Physical Chemistry: Gas Laws and Chemical Thermodynamics.

1. A  $1 \times 10^3$  L steel storage tank contains 88.5 kg of methane  $\text{CH}_4$ . If the temperature of the gas is 298 K determine the pressure inside the tank.
2. A sample of helium gas is held at constant temperature inside a cylinder of volume 0.80 L, where a piston exerts a pressure of  $1.5 \times 10^5$  Pa. If the external pressure on the piston is increased to  $2.1 \times 10^5$  Pa, what will the new volume of the gas be?
3. Calculate the work done by a system in which a reaction results in the formation of 1 mol  $\text{CO}_2$  gas at 298 K and 100 kPa. Assume that  $\text{CO}_2$  behaves as an ideal gas.
4. Calculate the work done when 1 mol Ar gas confined in a cylinder of volume  $1 \text{ dm}^3$  at 298 K expands isothermally and reversibly to  $2 \text{ dm}^3$ .
5. A strip of magnesium metal of mass 12.5 g is dropped into a beaker of dilute hydrochloric acid. Given that the Mg is the limiting reactant, calculate the work done by the system as a result of the reaction. The atmospheric pressure is 1 atm and the temperature is 293.2 K.

- A system absorbs 300 J of heat and at the same time expands by 1 dm<sup>3</sup> against a constant pressure of 1 atm. Determine the change in internal energy and enthalpy in the system. Note that 1 atm = 1.013 x 10<sup>5</sup> Nm<sup>-2</sup>.
- If the enthalpy of combustion of solid citric acid is – 1986 kJ mol<sup>-1</sup>, calculate the heat liberated when 10 g of solid citric acid undergoes total combustion at 298 K: (i) at constant pressure, (ii) at constant volume. Note: citric acid has formula C<sub>6</sub>H<sub>8</sub>O<sub>7</sub>. The molar mass M = 192 g mol<sup>-1</sup>. Total combustion means reaction with O<sub>2</sub> and conversion to CO<sub>2</sub> and H<sub>2</sub>O.

### **Problem Sheet 2.**

#### **Introduction to Physical Chemistry: Gas Laws and Chemical Thermodynamics.**

- Calculate the mole fraction of N<sub>2</sub>, O<sub>2</sub> and Ar in dry air at sea level, given that 100g of air consists of 75.5 g of N<sub>2</sub>, 23.2 g O<sub>2</sub> and 1.3 g Ar.
- Determine the mean free path of oxygen molecules in a sample of oxygen at SATP (298K, 1 bar) given that the collision cross section of oxygen is = 0.4 nm<sup>2</sup>.
- In an experiment to measure the heat released by the combustion of a sample of nutrient, the compound was burned in a calorimeter and the temperature was observed to rise by 3.22°C. When a current of 1.23 A from a 12 V source flows through a heater in the same calorimeter for a time of 156 s, the temperature rose by 4.47°C. What is the heat released by the combustion reaction?

4. Show that the difference in molar heat capacities for a perfect gas is given by:  $C_{P,m} - C_{V,m} = R$ .
5. Ethanol  $C_2H_5OH$  is brought to the boil at 1 atm. When an electric current of 0.682 A from a 12 V supply is passed for 500s through a heating coil immersed in the boiling liquid, it is found that the temperature remains constant but 4.33 g of ethanol is vaporized. What is the enthalpy of vaporization of ethanol at its boiling point at 1 atm?
6. The standard enthalpy of formation of gaseous water at 298 K is -241.82 kJ mol<sup>-1</sup>. Estimate its value at 373 K. Note that the molar heat capacities at constant pressure for  $H_2O(g)$ ,  $H_2(g)$  and  $O_2(g)$  are 33.58 JK<sup>-1</sup>mol<sup>-1</sup>, 28.84 JK<sup>-1</sup>mol<sup>-1</sup>, and 29.37 JK<sup>-1</sup>mol<sup>-1</sup> respectively.
7. Calculate the change in molar entropy when a sample of hydrogen gas expands isothermally to twice its initial volume.
8. Calculate the change in molar entropy when hydrogen gas is heated from 293K to 303K at constant volume. The molar heat capacity at constant volume for hydrogen is 22.44 JK<sup>-1</sup>mol<sup>-1</sup>.
9. Suppose a certain small bird has a mass of 30g. what is the minimum mass of glucose that it must consume to fly to a branch 10 m above the ground? The change in Gibbs energy the oxidation of 1 mol glucose ( $C_6H_{12}O_6$ ) to carbon dioxide and water vapour at 298K is - 2828 kJ.
10. Estimate the composition of a solution in which two isomers A and B are in equilibrium  $A \xrightleftharpoons{K} B$  at 37°C assuming that  $\Delta_r G^0 = - 2.2$  kJmol<sup>-1</sup>.

11. Calculate the equilibrium constant of the reaction  $\text{N}_2(\text{g}) + 3\text{H}_2(\text{g}) \rightarrow 2\text{NH}_3(\text{g})$  at 298K given that the change in standard Gibbs energy for the reaction is  $-32.90 \text{ kJmol}^{-1}$ .
12. Suppose that in an industrial process  $\text{N}_2$  at 1.00 bar is mixed with  $\text{H}_2$  at 3.00 bar and the two gases are allowed to come to equilibrium with the product ammonia in a reactor at constant volume in the presence of a catalyst. At the temperature of the reaction it has been determined experimentally that the equilibrium constant  $K = 977$ . What are the partial pressures of the three gases at equilibrium?

### Problem Sheet 3.

#### Chemical Equilibria and Electrochemistry

- 1.
- What do you understand by the terms weak acid and solution pH? Provide an example of a weak acid and indicate the way that the acid strength of a weak acid can be quantified.
  - Calculate the pH of a  $5.0 \times 10^{-2} \text{ M}$  NaOH solution given the information that  $K_w = 1.0 \times 10^{-14}$ .
  - Calculate the  $\text{H}_3\text{O}^+$  ion concentration and the pH of a  $0.003 \text{ M}$   $\text{Ba}(\text{OH})_2$  solution assuming that the ion product  $K_w = 1.0 \times 10^{-14}$ .
  - Derive an expression for the pH of an aqueous solution of weak acid HA of concentration  $c$  and having an acid dissociation constant  $K_A$ . If  $K_A$  is assumed to be very small derive an approximate expression for the solution pH mentioning any approximations which you make.



- e. Use the theoretical results derived in part c to calculate the pH of a weak acid solution of concentration 0.1 M and having an acid dissociation constant  $K_A = 3.5 \times 10^{-8}$ .
- f. Explain using chemical equations where pertinent, the observation that the pH of an aqueous sodium acetate solution is alkaline whereas the pH of an ammonium chloride solution is acidic.
- g. Explain using an example how a buffer solution works and derive an expression for the pH of a buffer solution containing a weak acid HA and its conjugate base  $A^-$ . Use this expression to calculate the pH of a solution containing 0.75 M lactic acid ( $K_A = 1.4 \times 10^{-4}$ ) and 0.25 M sodium lactate.

2.

- a. What do you understand by the terms equilibrium constant K and reaction quotient Q.
- b. Derive an expression which relates the change in reaction Gibbs energy  $\Delta G$  to the equilibrium constant K and the reaction quotient Q according to:  $\Delta G = RT \ln\left(\frac{Q}{K}\right)$ . Indicate how this expression may be used to relate the sign of  $\Delta G$  (and hence to the question of whether the reaction occurs in a spontaneous or non spontaneous manner) to the relative magnitudes of Q and K.
- c. The standard change in Gibbs energy for a chemical reaction at a temperature of 298 K is  $-150 \text{ kJ mol}^{-1}$ . Determine the equilibrium constant of the reaction.
- d. The following equation  $N_2(g) + O_2(g) \rightleftharpoons 2NO(g)$  describes the formation of NO which contributes to air pollution whenever a fuel is burnt in air in a closed container at a high temperature as in a gasoline engine. At 1500K the equilibrium constant  $K = 1 \times 10^{-5}$ . Suppose that a sample

of air has  $[N_2] = 0.80 \text{ mol dm}^{-3}$  and  $[O_2] = 0.20 \text{ mol dm}^{-3}$  before any reaction occurs. Calculate the equilibrium concentrations of reactants and products after the mixture has been heated to 1500K.

3.

- a. Briefly explain using specific examples and clearly labelled diagrams how a Galvanic (Voltaic) cell and how a Polymer Membrane Electrolyte (PEM) fuel cell operates.
- b. The net reaction that occurs in a voltaic cell is  $Zn(s) + 2Ag^+(aq) \rightarrow Zn^{2+}(aq) + 2Ag(s)$ . Write down the half reactions that occur at the anode and cathode. If the standard reduction potentials at 298K are  $E^0(Ag^+, Ag) = 0.799V$  and  $E^0(Zn^{2+}, Zn) = -0.763V$ , calculate the voltage developed by the cell, the change in reaction Gibbs energy  $\Delta G^0$  and the equilibrium constant  $K$  for the cell reaction. Is the reaction strongly product favoured?
- c. Consider a galvanic cell involving the following half-reactions:  $Ni^{2+}(aq) + 2e^- \rightarrow Ni(s)$ ,  $E^0(Ni^{2+}, Ni) = -0.25 V$ ;  $Cr^{3+}(aq) + 3e^- \rightarrow Cr(s)$ ,  $E^0(Cr^{3+}, Cr) = -0.74 V$ . Calculate the cell potential observed at a temperature of 298 K when  $[Ni^{2+}] = 1.0 \times 10^{-4}M$  and  $[Cr^{3+}] = 2.0 \times 10^{-3}M$ .
- d. In a large number of samples of water in which the copper ion concentration is expected to be quite small, the  $[Cu^{2+}]$  was measured using an electrochemical cell. This setup consisted of a silver electrode dipping into a 1.0 M solution of  $AgNO_3$ , which was connected by a salt bridge to a second compartment containing a copper electrode. The copper compartment was then filled with one water sample after another and the cell potential was measured for each sample. In the analysis of one particular sample the cell potential at 298 K was measured as 0.62 V, with the copper electrode being the anode. What was the

concentration of  $\text{Cu}^{2+}$  ion in this sample. Note that the relevant reduction potentials are  $E^0(\text{Cu}^{2+}, \text{Cu}) = 0.34 \text{ V}$  and  $E^0(\text{Ag}^+, \text{Ag}) = 0.80 \text{ V}$ .

- e. What mass of copper is deposited on the cathode of an electrolytic cell if an electric current of 2A is passed through a solution of  $\text{CuSO}_4$  for a period of 20 min.